Show your work. Answers alone get no credit.

$$k = 1.38 \times 10^{-23} \text{ J/K}$$

$$\sigma = 5.67 \times 10^{-8} \text{ W/m}^2 \cdot \text{K}^4$$

vater : $c = 4186 \text{ J/C}^\circ \cdot \text{kg}$ $\ell_f = 3.35 \times 10^5 \text{ J/kg}$
 $k = 9.0 \times 10^9 \text{ N} \cdot \text{m}^2/\text{C}^2$

{5} 1 Which circuit will draw more current from the battery?

v



- {10} 2 A capacitor with a capacitance of 4 Farads is charged to 7 volts.
 - (a) How much charge is on the capacitor?

(b) How much energy is stored in the capacitor?

- {10} **3** An amount of heat of 2093 Joules is added to 0.5 kg of water.
 - (a) How much does the temperature change?

(b) What is the **change** in the average kinetic energy of the water molecules?

- {5} 4 You have a chicken coop with a surface area of 6 square meters and walls that are 5cm thick. You plan to heat it with a lightbulb inside. The thermal conductivity of the walls is 0.05W/m·K. The temperature outside the box is 10°C. The chickens have asked for a temperature inside of 25°C. What wattage light bulb should you use to heat the coop?
- 5 The chickens have developed a micro-fusion-reactor in a steel can. The can is glowing red hot, with a temperature of 1000 Kelvin. The can has a surface area of 0.01 square meters and has an emissivity 0.88183. How much energy is radiated from the can per second?



{10} **6** The chickens are trying to melt the ice in their water bowl. They place an electrical heating element with a resistance of 2.5Ω in the bowl and run a current of 20A through the element. The heat from the element melts the ice. How much ice will melt in 335 seconds?



{10} 7 A 3kg chicken with a charge of -6C is drifting through outer space with a speed to 10 m/s as it passes through a region of space with an electric potential of 200 volts. Some time later the chicken passes through a region with an electric potential of 211 volts. What is the speed of the chicken in the 211 volt region?



- {5} 8 A chicken has charged a rat to -3 Coulombs and is repelling the rat with an electric field that creates a force on the rat of 15 Newtons to the east. What is the magnitude and direction of the electric field?
- {10} **9** Write equations sufficient to find the three currents.



{10} 10 Lines of equal electric potential are show in the graph. The electric potential of each line is labeled in volts.(a) Draw an arrow showing the direction of the electric field at the location of the small square.

(b) Compute the magnitude of the electric field at location of the small square.



{10} 11 In the pictured circuit the resistance is 20Ω , the capacitance is 0.3 Farad and $V_s = 12$ V. At time t = 0 the voltage on the capacitor is 20V. What will be the voltage 6 seconds later?



 $\{10\}$ **12** Find the electric field at the position of the square.



Solutions:

- {5} 1 Circuit A has the resistor in series while circuit B has the resistors in parallel. Parallel resistors have less effective resistance so the current will be greater in B.
- {10} **2**

(a)
$$Q = CV = (4\Sigma F)(7V) = 28C.$$

(b) $U = \frac{1}{2}QV = \frac{1}{2}CV^2 = 98J.$

{10} **3**

(a)
$$Q = mc\Delta T$$
 so
 $\Delta T = \frac{Q}{mc} = \frac{2093\text{J}}{(0.5\text{kg})(4186\frac{\text{J}}{C^{\circ}\text{,kg}})} = 1C^{\circ}$
(b) $\bar{K} = \frac{3}{2}kT$ so
 $\Delta \bar{K} = \frac{3}{2}k\Delta T = \frac{3}{2}k(1C^{\circ}) = 2.07 \times 10^{-23}\text{J}.$

$$\{5\} \quad \mathbf{4} \ P = kA\frac{\Delta T}{\Delta x} = \left(0.05\frac{W}{\text{m}\cdot C^{\circ}}\right)(6\text{m}^2)\frac{25^{\circ}C - 10^{\circ}C}{(0.05\text{m})}\text{W} = 90\text{W}.$$

{5} **5**
$$P = \sigma \epsilon A T^4$$
 so
 $P = (5.67 \times 10^{-8})(0.88183)(0.01)(1000)^4 W = 500 W.$

{10} **6** If we let the amount of water melted be *m* then the amount of heat absorbed is. $Q = m\ell_f$ while the amount of heat emitted by the resistor is $Q = P\Delta t = IV\Delta t = I^2R\Delta t$. Thus $m = \frac{Q}{\ell_f} = \frac{I^2R\Delta t}{\ell_f} = 1.0kg$

{10}
$$7 \Delta K + \Delta U = 0 \rightarrow \frac{1}{2}m(v_f^2 - v_i^2) + q(V_f - V_i) = 0$$
 Thus
 $v_f = \sqrt{v_i^2 - \frac{2q}{m}(V_f - V_i)}$
 $= \sqrt{10^2 - \frac{2(-6)}{3}(211 - 200)} \frac{m}{s} = 12\frac{m}{s}$

{5} 8 $\vec{E} = \frac{\vec{F}}{q} \to |E| = \frac{|F|}{|q|} = 5$ N/C, west.

{10} 9
$$I_1 - I_2 - I_3 = 0$$

-(3 Ω) $I_1 + 5V - (7\Omega)I_2 = 0$
(2 Ω) $I_3 - 9V - (7\Omega)I_2 = 0$

$$\{10\}$$
10 $|E| = \left|\frac{\Delta V}{\Delta r}\right| = \frac{3V}{1.5m} = 2.0$ V/m.



{10} **11** $V_C(t) - V_s = (V_C(0) - V_s)e^{-t/RC}$ so $V_C(6s) - V_s = (20V - 12V)e^{-6s/6s} = 2.9V$ so $V_C(6s) = V_s + 2.9V = 14.9V.$

 $\{10\}$ **12** First find magnitudes.

$$E_{1} = k \frac{|q_{1}|}{r_{1}^{2}} = 9 \times 10^{9} \frac{13 \times 10^{-9}}{3^{2} + 2^{2}} \frac{N}{C} = 9 \frac{N}{C}$$

$$E_{2} = k \frac{|q_{2}|}{r_{2}^{2}} = 9 \times 10^{9} \frac{9 \times 10^{-9}}{3^{2} + 0^{2}} \frac{N}{C} = 9 \frac{N}{C}$$

$$z \int \frac{1}{E_{1}} \frac{1}{r_{2}} \frac{1}{r_{2$$

Instructions:

Do your work on separate blank paper. Put this sheet on top and staple them all together. Use only this exam sheet and a calculator.